

The crystal structure of synthetic chukhrovite, $\text{Ca}_4\text{AlSi}(\text{SO}_4)\text{F}_{13} \cdot 12\text{H}_2\text{O}$

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Abstract

Synthetic chukhrovite, $\text{Ca}_4\text{AlSi}(\text{SO}_4)\text{F}_{13} \cdot 12\text{H}_2\text{O}$ crystallizes in the cubic space group $Fd\bar{3}$, with $a = 16.710(2)\text{\AA}$ and $Z = 8$. The structure was refined to $R_w = 0.028$ and $R = 0.025$, using 481 nonzero reflections.

Al and Si are statistically distributed at the same site, M [16(d)], which is surrounded by six fluorine atoms to form the octahedral group MF_6 . The remaining fluoride ion is surrounded by a tetrahedron of Ca ions [F(1)-Ca = 2.411\AA] as in fluorite. The overall coordination of Ca is seven with a geometry corresponding to that of a monocapped octahedron. Each corner of the MF_6 octahedron is linked to a Ca coordination polyhedron and each Ca polyhedron shares three corners with three different MF_6 octahedra. The SO_4 ion is surrounded by 12 water molecules, all of which are hydrogen-bonded to SO_4 oxygens. The most unusual feature of this hydration is that all four faces of the SO_4 ion are linked to faces of Ca polyhedra via hydrogen bonding.

Introduction

The mineral chukhrovite occurs in the secondary oxidation zone of the Kara-Oba molybdenum-tungsten deposit in central Kazakhstan. These crystals have been described as face-centered cubic with $a = 16.80\text{\AA}$, crystal class $T_h = m\bar{3}$, and with typical octahedral habit (Ermilova *et al.*, 1960). The chemical composition was given as: $\text{Ca}_3\text{Al}_2(\text{Y,RE})\text{SO}_4\text{F}_{13} \cdot 10\text{H}_2\text{O}$, where RE may be a mixture of rare-earth elements.

Crystals of similar composition and X-ray diffraction pattern to that of the mineral chukhrovite often occur in the filter cake during the manufacture of phosphoric acid. Lehr *et al.* (1966) and Coates and Woodard (1966) have published detailed descriptions of this mineral. Coates and Woodard suggested that these octahedral crystals are isomorphous with chukhrovite. They reported a cell parameter of $16.75(5)\text{\AA}$, space group $Fd\bar{3}$, and gave the chemical composition as: $\text{Ca}_{4.03}\text{Ba}_{0.04}(\text{Y,La})_{0.09}\text{Al}_{1.31}\text{Si}_{0.75}(\text{SO}_4)_{1.00}\text{F}_{13.0} \cdot 10\text{H}_2\text{O}$. Meredith (1965), in his studies

of the reaction of hydrochloric acid with phosphate rock, reported a residual crystalline material with the formula $\text{CaSO}_4 \cdot 1.5\text{CaSiF}_6 \cdot \text{AlF}_3 \cdot \text{CaF}_2 \cdot 12\text{H}_2\text{O}$. The X-ray diffraction pattern and the differential thermal and thermogravimetric analysis reported by Meredith show that this material is similar to our synthetic chukhrovite. Hájek and Benda (1972) reported a synthetic material with the chemical composition $\text{Ca}_{12}\text{Al}_2\text{Si}_4(\text{SO}_4)_3\text{F}_{40} \cdot 45\text{H}_2\text{O}$ which corresponds to $\text{Ca}_4\text{Al}_{0.67}\text{Si}_{1.33}(\text{SO}_4)\text{F}_{13.3} \cdot 15\text{H}_2\text{O}$. Again, these are octahedral crystals with cubic symmetry and on the basis of the X-ray diffraction pattern appear to be quite similar to our synthetic chukhrovite.

Experimental

Our crystals of synthetic chukhrovite were prepared as part of a factorial-designed experiment to study the effect of F, Al, and Si on the precipitation of chukhrovite (Frazier *et al.*, 1977). In one of these trials exceptionally large octahedral crystals of chukhrovite were obtained (up to $200\ \mu\text{m}$ along a) by

Table 3.

Observed and calculated structure factors for $\text{Ca}_4(\text{Al}_2, \text{Si})\text{SO}_4\text{F}_{13} \cdot 12 \text{H}_2\text{O}$. The columns L, O, and C are the values of λ , $10 F_0$ and $10 F_c$ respectively. Reflections with $F_0 < 3\sigma(F_0)$ are considered unobserved and are marked by *.

L	O	C	L	O	C	L	O	C	L	O	C
	1,1,L		2 450		501	4 2613		2625	2 983		-1026
			4 841		-853	6 830		-823	6 67*		-81
1 3557		3449		6,4,L			8,6,L			10,2,L	
	2,2,L		2 4481		-4453	2 1806		1874	0 783		766
0 3115		-3093	4 1488		-1503	4 914		-879	2 2581		2590
2 414		-436		6,6,L		6 51*		69	4 774		750
	3,1,L		0 3926		-3938		8,8,L		6 3460		3513
1 2023		-2011	2 2298		2240	0 2928		2899	8 1708		-1715
	3,3,L		4 1765		-1774	2 1892		1930		10,4,L	
1 1351		1348	6 583		-532	4 1106		1091	2 331		-331
3 345		347		7,1,L		6 443		433	4 2273		-2212
	4,0,L		1 2371		2451	8 956		975	6 2389		-2381
0 4050		4196	3 505		-485		9,1,L		8 137*		95
	4,2,L		5 1068		1051	1 1473		1447		10,6,L	
1 1709		1651		7,3,L		3 1549		-1596	0 723		739
	4,4,L		1 4938		4797	5 1269		1241	2 236		-202
2 1709		1651	3 91*		63	7 653		-617	4 1051		-1071
	5,1,L		5 641		598		9,3,L		6 630		604
0 1973		1942		7,5,L		1 1944		-1951	8 1187		1215
2 755		838	1 418		-378	3 3319		-3339		10,8,L	
4 1046		-995	3 1401		-1380	5 710		-667	2 967		-969
	5,3,L		5 1146		1181	7 805		-784	4 2424		-2388
1 3583		3539		7,7,L			9,5,L		6 1294		1276
3 2888		-2867	1 306		-287	1 441		437	8 215		-246
	5,5,L		3 1351		1344	3 2311		2357		10,10,L	
1 183		-122	5 3195		-3202	5 1149		1172	0 2240		-2284
3 4223		-4250	7 1018		998	7 50*		-20	2 698		-707
	6,0,L			8,0,L			9,7,L		4 567		531
1 1067		1117	0 2064		-2012	1 1297		-1297	6 740		740
3 3008		2904	4 2146		-2124	3 2487		-2477	8 430		457
5 4179		4244		8,2,L		5 1002		-1011	10 2926		2997
	6,2,L		2 246		203	7 934		-973		11,1,L	
2 3057		-2994	4 3237		3208		9,9,L		1 229		-167
	6,4,L		6 1436		1440	1 716		-696	3 1920		-1965
0 3067		2944		8,4,L		3 1334		1362	5 208		-177
			0 311		-306	5 1053		1028	7 2537		-2574
			2 4832		4783	7 177		62	9 660		-670
						9 494		449		11,3,L	
							10,0,L		1 402		-405
									3 911		903

L O C			L O C			L O C			L O C		
11.3.L			12.6.L			13.7.L			14.6.L		
5	1159	-1140	2	507	500	1	1287	-1311	0	690	-679
7	168	-175	4	1419	-1460	3	518	-509	2	1105	1113
9	549	518	6	3412	3336	5	1197	-1178	4	1098	1097
			8	432	-421	7	343	347	6	854	863
			10	1090	1134	9	752	-769	8	555	-557
11.5.L			12.8.L			13.9.L			14.8.L		
1	684	692									
3	265	-260	0	248	227	1	544	519	2	590	581
5	369	352	2	1406	-1477	3	1527	1560	4	1585	-1585
7	1741	-1784	4	2083	2128	5	630	610	6	1012	-992
9	363	412	6	212	153	7	116*	107	8	1062	-1074
			8	397	-407	9	814	781	10	240	-222
11.7.L			10	52*	15	11	659	-696	12	142*	-93
1	2403	-2408	12.10.L			13.11.L			14.10.L		
3	636	622									
5	1428	-1450	2	766	785	1	46*	41	0	550	525
7	618	-606	4	296	-270	3	219	175	2	601	-584
9	126*	72	6	386	384	5	900	-898	4	57*	-28
			8	115*	141	7	496	504	6	318	323
11.9.L			10	738	740	9	720	-719	8	653	652
1	297	-298	12.12.L			11	160*	109	10	1714	1735
3	2198	2180				13.13.L			12	839	-810
5	935	-944	0	2550	2606				14.12.L		
7	233	-162	2	139*	135	1	250	208			
9	828	-801	4	456	433	3	341	351	2	929	-946
			6	559	517	5	1315	1326	4	308	271
11.11.L			8	112*	36	7	131*	136	6	162*	-196
1	908	-867	10	220	146	9	573	578	8	227	-150
3	100*	62	12	793	-763	11	231	-175	10	1003	-963
5	1425	-1443	13.1.L			13	352	341	12	82*	15
7	1118	-1142				14.0.L			14.14.L		
9	966	-992	1	1690	-1695						
11	201	-155	3	1431	-1443	2	2388	2442	0	614	-679
			5	1451	-1488	6	1572	1642	2	89*	27
12.0.L			7	2691	-2766	10	1261	1293	4	396	417
0	1652	-1617	9	573	567	14.2.L			6	247	226
4	611	611	11	985	-970				8	451	-421
8	839	852	13.3.L			0	335	309	10	1187	1177
						2	2397	2423	12	55*	27
12.2.L			1	88*	52	4	1022	-1025	15.1.L		
2	1744	1754	3	1417	-1401	6	950	920			
4	677	687	5	1214	-1240	8	66*	-65	1	376	-377
6	1119	1095	7	484	-496	10	801	-820	3	1078	-1069
8	369	-354	9	202	193	12	1224	-1209	5	409	-408
10	1836	1871	11	102*	115	14.4.L			7	583	-586
			13.5.L						9	86*	57
12.4.L						2	244	258	11	190	-141
0	1248	1263	1	157*	-144	4	1665	-1630	13	671	-676
2	800	810	3	911	-929	6	1517	1507	15.3.L		
4	507	525	5	455	-442	8	157*	-90			
6	169	70	7	1219	-1226	10	465	-464	1	1662	-1672
8	1933	1994	9	726	722	12	153*	-23			
10	308	-295	11	1887	-1903						

L	O	C	L	O	C	L	O	C	L	O	C
	18.4.L			19.3.L			20.2.L		5	1151	-1160
8	150*	-181	1	336	-333	2	769	764	7	423	448
10	560	546	3	819	808	4	954	-966	9	1055	-1088
12	478	-454	5	126*	-191	6	453	-469		21.5.L	
14	275	-319	7	503	489	8	1042	-1041			
	18.6.L		9	253	227	10	113*	-113	1	169*	200
0	1904	1895	11	481	469	12	222	-154	3	649	-635
2	1565	1550	13	304	-293		20.4.L		5	158*	-135
4	553	530		19.5.L		0	1856	1802	7	166*	-193
6	496	453	1	964	-961	2	778	-764	9	453	-418
8	162*	-145	3	247	-281	4	180*	87		21.7.L	
10	436	442	5	1332	-1352	6	192*	241	1	320	-282
12	1569	-1587	7	696	685	8	182*	156	3	349	315
	18.8.L		9	583	-573	10	611	616	5	353	-312
2	682	-626	11	143*	137		20.6.L		7	214*	-161
4	343	-313		19.7.L		2	347	-354		21.9.L	
6	312	-259	1	326	328	4	457	418	1	498	475
8	417	-398	3	96*	6	6	333	-319	3	875	-883
10	775	-770	5	623	604	8	296	266	5	224	-224
12	56*	-4	7	1076	1092	10	881	-903		22.0.L	
	18.10.L		9	105*	-67		20.8.L		2	582	559
0	455	443	11	418	401	0	364	372	6	97*	15
2	438	425		19.9.L		2	260	-262		22.2.L	
4	799	798	1	297	-268	4	840	816		22.2.L	
6	397	371	3	227*	176	6	222*	249	0	1000	1019
8	867	-830	5	884	-889	8	213*	-217	2	286	-277
10	499	444	7	153*	-185		20.10.L		4	137*	-26
	18.12.L		9	1079	-1090	2	63*	42	6	580	577
2	536	-524		19.11.L		4	876	843		22.4.L	
4	423	428	1	450	467	6	816	-799		22.4.L	
6	1531	-1512	3	265	-223		20.12.L		2	174*	-180
8	177*	161	5	134*	-108	0	124*	-82	4	1106	1096
	18.14.L		7	550	537	2	205*	-220	6	683	679
0	420	-437		19.13.L			21.1.L			22.6.L	
2	467	467	1	777	772	0	508	489		22.6.L	
4	588	-568	3	153*	-59	2	521	548		22.6.L	
	19.1.L			20.0.L		1	474	506	4	521	540
1	924	-989	0	948	979	3	533	504		23.1.L	
3	94*	-87	4	1268	1291	5	533	534		23.1.L	
5	134*	-113	8	238	221	7	227	212	1	427	-442
7	85*	128	12	528	517	9	839	831	3	353	-410
9	67*	-84					21.3.L			23.3.L	
11	110*	26				1	40*	30		23.3.L	
13	191*	206				3	502	470	1	500	-519